

## DOES ENERGY AND IMPULSE ARE INTER CONVERTABLE

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**Abstract:** Consider a photon of relativistic mass ' $m$ ' moving with speed ' $c$ ' is associated with the wavelength ' $\lambda$ ' is given by the relation  $\lambda = h/mc$ , Where  $h = \text{planck's constant } (6.625 \times 10^{-34} \text{ JS})$ . According to **wave theory**, speed of the photon wave is given by  $c = \lambda / T$ , where  $T =$  time period. By substitution of value of ' $c$ ' in the equation  $\lambda = h/mc$ , we get the expression  $m \lambda^2 = hT$ . According to **wave theory**, as frequency of photon wave is given by  $f = 1/T$ . [Academia Arena, 2010;2(5):15-18] (ISSN 1553-992X).

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According to **wave theory**, speed of the photon wave is given by  $c = \lambda / T$ , where  $T =$  time period.

By substitution of value of ' $c$ ' in the equation  $\lambda = h/mc$ , we get the expression  $m \lambda^2 = hT$ .

According to **wave theory**, as frequency of photon wave is given by  $f = 1/T$ .

Then the equation  $m \lambda^2 = hT$  becomes  $f = h/m\lambda^2$

De Broglie wavelength associated with the photon is given by  $\lambda = h/p$ ,

thus the equation  $f = h/m\lambda^2$  becomes  $f = p/m\lambda$ .

Angular frequency associated with the photon is given by  $\omega = 2 \pi f$ .

By putting the value of  $f = p/m\lambda$  in the above equation we get  $\omega = 2 \pi p/m\lambda$ .

The above equation  $\omega = 2 \pi p/m\lambda$  can be applied to both photons and material particles like electron in motion.

Debroglie wavelength associated with the electron is given by  $\lambda = h/mv$

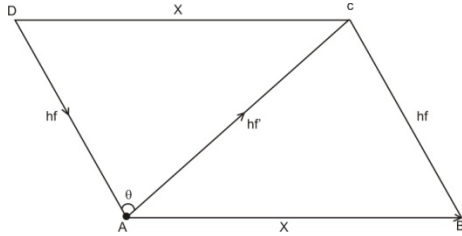
Where  $v =$  velocity of electron in motion

Then the equation  $\omega = 2 \pi p/m\lambda$  becomes  $\omega = 2 \pi p m v / m h$  i.e  $\omega = 2 \pi v / h$ .

### Part : 2

Consider a electron of mass " $m_e$ " at rest, total energy associated with the electron is given by " $m_e c^2$ ". Suppose radiation of energy  $hf$  is incident on this electron at rest. Part of energy  $hf$  is absorbed by electron and part of

energy  $hf$  is scattered by electron . Absorbed energy  $hf'$  is converted to motion of electron, hence electron travels a distance ' $x$ ' in time ' $t$ '. let  $\theta$  is the scattering angle.



**Figure :1** –schematic diagram of scattering of energy of photon by electron

$x$ = Linear displacement of electron

$hf$  = Energy of incident radiation

$hf'$  = Energy of scattered radiation

$\theta$  = scattering angle

Consider a parallelogram ABCD constructed as shown in the figure 1.

Let  $AB=CD=x$ ,  $AD=BC=hf$ ,  $AC=hf'$  (opposite sides in parallelogram are equal)

Law of cosine is given by  $a^2=b^2+c^2-2bc \cos \theta$ . Let  $a = x$ ,  $b=hf$ ,  $c=hf'$ ,  $\cos A = \cos\theta$ .

By applying the law of cosine to the triangle ADC, we get

$$X^2=(hf)^2+(hf')^2-2(hf)(hf') \cos \theta = 1$$

By law of conservation of momentum of photon.

We get  $\vec{p}_y = \vec{p}_{y''} + \vec{p}_{y'}$  where  $\vec{p}_y, \vec{p}_{y''}, \vec{p}_{y'}$  be the momentum of incident, absorbed and scattered photon respectively.

Let us assume absorbed momentum of photon = momentem of electron

i.e.  $\vec{p}_{y''} = \vec{p}$

Thus  $\vec{p}_y = \vec{p}_{y''} + \vec{p}_{y'}$  where  $\vec{p}$  = momentum of electron

$\vec{p}_y = \vec{p}_{y''} + \vec{p}_{y'}$  Squaring on the both sides we get

$$P^2 = \left( \begin{matrix} \vec{p} & \vec{p} \\ y & y' \end{matrix} \right)^2, \text{ as } (a-b)^2 = a^2 + b^2 - 2ab$$

Thus the above equation becomes  $p^2 = p_y^2 + p_{y'}^2 - 2 \left| \vec{p}_y \cdot \vec{p}_{y'} \right|$

According to dot product rule  $\left| \vec{a} \cdot \vec{b} \right| = |\vec{a}| |\vec{b}| \cos \theta$

Then we get  $p^2 = p_y^2 + p_{y'}^2 - 2 \left| p_y \right| \left| p_{y'} \right| \cos \theta$

Let us multiply the above equation by  $c^2$  we get

Where  $c$  = speed of light in vacuum ( $3 \times 10^8$  m/s)

$$P^2 c^2 = p_y^2 c^2 + p_{y'}^2 c^2 - 2 \left| p_y \right| \left| p_{y'} \right| c^2 \cos \theta$$

As we know frequency of photon is directly proportional to its momentum

i.e  $hf = pc$  thus the below equation is obtained

$$p^2 c^2 = (hf)^2 + (hf')^2 - 2(hf)(hf') \cos \theta = 2$$

By comparison of 1 and 2 we get  $x^2 = p^2 c^2$

i.e  $x = pc$  (position of electron is defined as the function of its momentum)

As told earlier position of electron is defined as a function of its momentum i.e  $x = pc$

Small change in momentum of electron causes small change in its position i.e.  $dx = dp c$  hence,

$$dp = dx/c$$

**Newton second law of motion** is mathematically represented by equation  $F = dp/dt$

Where  $F$  = force exerted by photon

$dp$  = Small change in momentum of electron with respect to time

As  $dp = dx/c$  then the above equation becomes  $F = dx/dtc$ .

as velocity of electron is defined as  $v = dx/dt$ .

Then  $F = v/c$  is obtained

Force exerted by photon is defined as function of velocity of electron

As impulse exerted by photon is mathematically given by  $I = F dt$ .

then the equation  $F = dx/dtc$  becomes  $F dt = dx/c$

i.e  $I = dx/c$

Impulse exerted by photon is defined as function of change in position of electron

At point A and B mass of electron is  $m_e$ . i.e total energy associated with electron is  $mc^2$ . (as electron is at rest at

point A and B)

But in between point A and B mass of electron is  $mc^2$  (since electron is in motion in between point A and B )

Hence total energy of electron in motion is mathematically given by  $E = mc^2 + hf$

(As absorbed energy adds up to rest mass energy ) where  $E$  = total energy of electron in motion

$hf$  = absorbed energy of photon

$mc^2$  = rest mass energy of electron

As absorbed momentum of photon equals the momentum of electron i.e  $p_{\gamma} = p$

As  $x = pc$  (position of electron is defined as the function of it's momentum) then  $x = p_{\gamma}c$

$p_{\gamma}c = hf$  then  $x = hf$  then the equation  $E = mc^2 + hf$  becomes equation  $E = mc^2 + x$

According to Einstein equation  $E = mc^2 + E_k$

By comparison of 3 and 4 we get  $E_k = x$  i.e kinetic energy of electron = position of electron

Small change in kinetic energy of electron causes small change in it's position i.e  $dE_k = dx$  i.e  $I = dx/c$

i.e  $I = dE_k/c$  i.e  $dE_k = Ic$

According to workenergy theorem

Work done on particle equals change in kinetic energy of particle i.e  $W = dE_k$  i.e  $W = Ic$

Work done on particle involves storage of energy in particle i.e  $W = E_a$  where  $E_a$  = Energy stored in particle.

$E_a = Ic$ , energy stored in particle is defined as a function of impulse applied

Thus  $E_a = I c$  (as  $c$  is constant ) i.e impulse and energy are interconvertable.

## 2) Proof for Einstein predicted formula $E = tc$

As  $x = pc$  (position of electron is defined as the function of it's momentum)

As momentum of electron can be given by  $p = mv$  then the equation  $x = pc$  becomes  $x = mvc$  i.e  $x/v = mc$

According to Newton  $v = x/t$  i.e equation  $x/v = mc$  becomes  $t = mc$

According to Einstein  $E = mc^2$  hence  $E = mcc$  becomes  $E = tc$

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