

## There are finite Mersenne primes and There are finite repunits primes

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**Abstract:** Using Jiang function we prove the finite Mersenne primes and the finite repunits primes.

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**Theorem.** Suppose the prime equation

$$P_1 = \frac{(P-1)^{P_0} - 1}{P-2} \quad (1)$$

where  $P_0$  is a given prime.

There exist infinitely many primes  $P$  such that  $P_1$  is a prime.

**Proof.** We have Jiang function [1]

$$J_2(\omega) = \prod_P [P-1 - \chi(P)] \quad (2)$$

where  $\omega = \prod_P P$ ,  $\chi(P)$  is the number of solutions of congruence

$$\frac{(q-1)^{P_0} - 1}{q-2} \equiv 0 \pmod{P} \quad , \quad q = 1, \dots, P-1 \quad (3)$$

$$\chi(P_0) = 1 \quad , \quad \chi(P) = P_0 - 1 \quad \text{if } P \equiv 1 \pmod{P_0} \quad , \quad \chi(P) = 0 \quad \text{otherwise.}$$

Since  $J_2(\omega) \neq 0$ , there exist infinitely many primes  $P$  such that  $P_1$  is a prime.

We have the asymptotic formula [1]

$$\pi_2(N, 2) = \left| \{P \leq N : P_1 = \text{prime}\} \right| \sim \frac{1}{P_0 - 1} \frac{J_2(\omega)\omega}{\phi^2(\omega)} \frac{N}{\log^2 N} \quad (4)$$

$$\text{where } \phi(\omega) = \prod_P (P-1)$$

Let  $P = 3$ . From (1) we have equation of Mersenne numbers [2]

$$P_1 = 2^{P_0} - 1 \quad (5)$$

From (4) we have

$$\pi_2(3, 2) = \left| \{3 \leq N : 2^{P_0} - 1 = \text{prime}\} \right| \sim \frac{1}{P_0 - 1} \frac{J_2(\omega)\omega}{\phi^2(\omega)} \frac{3}{\log^2 3} \rightarrow 0 \quad \text{as } P_0 \rightarrow \infty \quad (6)$$

We prove the finite Mersenne primes.

Let  $P = 11$ . From (1) we have equation of repunits numbers [2]

$$P_1 = \frac{10^{P_0} - 1}{9} \quad (7)$$

From (4) we have

$$\pi_{11}(11, 2) = \left| \left\{ 11 \leq N : \frac{10^{P_0} - 1}{9} = \text{prime} \right\} \right| \sim \frac{1}{P_0 - 1} \frac{J_2(\omega)\omega}{\phi^2(\omega)} \frac{11}{\log^2 11} \rightarrow 0$$

as  $P_0 \rightarrow \infty$ . (8)

We prove the finite repunits primes.

In the same way we are able to prove that  $\frac{(a^{P_0} - 1)}{(a - 1)}$  with  $a = 4, 6, 10, 12, \dots$ , has the finite prime solutions.

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