## Practice and Understanding of the Goldbach Problem（A）

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#### Abstract

Practice shows：Without enough parameters， $1+2$ cannot estimate $1+1$ and $1+1 \times 1$ ．At the same time，it is pointed out that among the prime numbers not greater than N ，the prime number $6 \mathrm{t}-1$ is more than the prime number $6 \mathrm{t}+1$ ，（this is the＂detail＂that Hardy and the others did not notice．）＂detail＂（＝＂remainder＂）affects Represents the negligible oscillation in the accuracy curve of the number $\mathrm{r} 2(\mathrm{~N}$ ）of Hardy－Litttlewood conjecture（A）in 1921．（In 1989， Hua Luogeng（华罗庚）confirmed that conjecture（A）is the＂main term＂of even Goldbach＇s problem．） ［Tong Xinping（童信平）Practice and Understanding of theGoldbachProblem（A）AcademArena2021；13（4）：71－75］． ISSN1553－992X（print）；ISSN2158－771X（online）．http：／／www．sciencepub．net／academia．7．doi：10．7537／marsaaj130421． 07.


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In 1977，from a logical and philosophical point of view，I thought that＂ $1+2$＂could not reach＂ $1+1$＂（short for even Goldbach conjecture）．Starting from interest，I am determined to find mathematical evidence that＂ $1+2$＂ cannot reach＂ $1+1$＂under the guidance of philosophical viewpoints．Seeing Xu Chi＇s article，I dare not act． However，the passion in my heart cannot be extinguished． After waiting for 4 years，in 1981，finally in some books， the Pan brothers said：＂It is impossible to prove the proposition $\{1,1\}$ by using Chen Jingrun＇s weighted sieve method．＂＂The coefficient value of（＇1＋2＇），It may be more than 2 to be valuable．＂Wang Yuan（王元）said： ＂It is impossible to prove $(1,1)$ with the improvement of the current method．＂They partially admitted that Hardy said in 1921 that＂Goldbach＇s conjecture does not seem to be able to use Brown＇s Method to prove＂．With these speeches，I can move forward，and under the encouragement of the spirit of＂everyone is responsible＂， find a new way to relieve the Chinese people＇s pain of not being able to prove＂ $1+1$＂．I believe that we can use mathematical practice $\rightarrow$ knowledge，practice again $\rightarrow$ recognize again this magic weapon of crossing the river by touching the stones，complete the following three experimental verifications，and get a new understanding of＂ $1+1$＂．

1 The formula（Ca）is Chen Jingrun＇s＂1＋2＂．Practice shows：＂1＋2＂lacks parameter 2 and cannot be used to calculate＂ $1+1$＂．
（Ca）
$\mathrm{r}_{2}(\mathrm{~N})>0.67 \mathrm{c}(\mathrm{N}) \frac{N}{\ln ^{2} N} \Pi \frac{\mathrm{p}-1}{\mathrm{p}-2}=2 \mathrm{c}(\mathrm{N}) \frac{N}{\ln ^{2} N} \Pi$
$\frac{\mathrm{p}-1}{\mathrm{p}-2}(1-0.665)$ 。

The $\mathrm{c}(\mathrm{N})$ in the formula is represented c in the other book．

Wang Yuan said that to prove＂ $1+1$＂is to prove $(1+\mathrm{O}(1)) \rightarrow 1$ ，which is the＂remainder＂ $\mathrm{O}(1) \rightarrow 0$ ．The -0.665 here is a definite value，not $\rightarrow 0$ ，and it cannot be called＂remainder＂．This can be simply explained mathematically，what is calculated with＂ $1+2$＂is not ＂ $1+1$＂．

So，let＇s assume that the coefficient value is greater than 2.67 ，is it more useful？Please see the formula（ Cb ）； （Cb）
$\mathrm{r}_{2}(\mathrm{~N})>2.67 \mathrm{c}(\mathrm{N}) \frac{N}{\ln ^{2} N} \Pi \frac{\mathrm{p}-1}{\mathrm{p}-2}=2 \mathrm{c}(\mathrm{N}) \frac{N}{\ln ^{2} N} \Pi \frac{\mathrm{p}-1}{\mathrm{p}-2}$ $(1+0.335)$

Here is 0.335 ，it is not $\rightarrow 0$ ，and the more it is greater than 2 ，it is cannot $\rightarrow 0$ ．－Greater than 2 has no value．

On February 13，1992，at the press conference of the Institute of Mathematics，Wang Yuan said to the media： ＂Chen Jingrun never proved $1+1$ ，and never even thought that he could prove $1+1$ ．＂Therefore，Chen Jingrun is want to prove＂ $1+2$＂，but he didn＇t to prove＂ $1+1$＂in the past．How is it possible to get＂ $1+1$＂？

2 Formula（III）can calculate＂ $1+1 \times 1$＂．Practice shows： ＂1＋2＂lacks parameters and cannot be used to calculate＂ $1+1 \times 1$＂．

Figure 1 is the experimental accuracy curve of formula（III）and formula（Ca）．
（III）
$\mathrm{N}(1,1 \times 1)_{\mathrm{m}} \sim \frac{2 \pi(\mathrm{~m})(\pi(\mathrm{N})-\mathrm{r}+1)}{\mathrm{N}} \Pi\left(1-\frac{1}{(\mathrm{p}-1)^{2}}\right) \Pi \frac{\mathrm{p}-1}{\mathrm{p}-2} \sum$

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\((\mathrm{p}-1)+\ldots\)
\(\mathrm{p}(\mathrm{p}-2)\)
\(\underset{3 \leqslant p \leqslant \sqrt{ } \mid \mathrm{N}}{\underset{3}{ } \nmid \mathrm{~N}}\)
\(3 \leqslant p \leqslant \sqrt{ } N \quad 3 \leqslant p \leqslant \sqrt{ } N\)
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Figure 1 shows that within the experimental range, formula (III) is far more accurate than formula (Ca). The main reason is that the formula $(\mathrm{Ca})$ has no parameter $\Sigma$ $(\mathrm{p}-1) \mathrm{p}(\mathrm{p}-2)$. It can be seen that " $1+2$ " $=$ formula $(\mathrm{Ca}) \neq$ formula (III), " $1+2$ " cannot be used to calculate " $1+1 \times 1$ ".

The above analysis shows that " $1+2$ " can contain " $1+1$ " and $" 1+1 \times 1$ ". However, it cannot be said separately that $" 1+2$ " proves $" 1+1$ " or $" 1+1 \times 1$ ". Here, " $1+2$ " can be compared to the compound water $(=\mathrm{H} 2 \mathrm{O})$ that can extinguish fire. We cannot separate H 2 O . Water

$$
\mathrm{r}_{2}(\mathrm{~N}) \sim\left[2 \frac{\pi\left(N-p_{r}-1\right)(\pi(N)-r+1)}{N} \quad \Pi \quad\left(1-\frac{1}{(\mathrm{p}-1)^{2}}\right)\right]
$$

In formula (3), when $\mathrm{N} \rightarrow \infty, \pi(\mathrm{N}-\mathrm{pr}-1) \rightarrow \pi(\mathrm{N})$. $\pi(N)-r-1 \rightarrow \pi(N) . r /(\pi(N)-r-1) \rightarrow 0$, the formula (2) is obtained.

When the "remainder" $\pm \delta$ is not included, formula (2) is the Hardy-Littlewood conjecture (A) in 1921.
$\mathrm{r}_{2}(\mathrm{~N}) \sim 2 \frac{\pi^{2}(N)}{N} \Pi\left(1-\frac{1}{(\mathrm{p}-1)^{2}}\right) \Pi \frac{\mathrm{p}-1}{\mathrm{p}-2}(1 \pm \delta)$
According to the prime number theorem $\frac{\pi^{2}(N)}{N} \sim \frac{N}{\ln ^{2} N}$, Get formula (1)。
(1)

$$
\mathrm{r}_{2}(\mathrm{~N}) \sim 2 \frac{N}{\ln ^{2} N} \Pi\left(1 \frac{1}{(\mathrm{p}-1)^{2}}\right) \Pi \frac{\mathrm{p}-1}{\mathrm{p}-2}(1 \pm \delta)
$$

In 1989, Hua Luogeng used "A Direct Attempt to Goldbach Problem" to proof his mentor Hardy conjecture (A) obtained by through hypotheses, further proving that the conjecture (A) is the "main term" of the even Goldbach conjecture. Therefore, what remains to be studied is the unresolved "remainder" $\pm \delta$, (Hardy called it "details" at the time.)

That prime numbers greater than 2 and 3 can be divided into: prime number $\mathrm{p}_{\mathrm{E}}=6 \mathrm{t}-1$ and prime number p ${ }_{+}=6 \mathrm{t}+1$. In the N , the $\mathrm{p}_{-}$is more and $\mathrm{p}_{+}$is less. Therefore, p. and $p_{+}$are the real parameters. If the $\mathrm{N}=6 \mathrm{n}-2=\mathrm{p}_{-}+\mathrm{p}_{\text {., }}$,
is H 2 (combustible) or O (combustion-supporting). More generally speaking, " $1+2$ " is like Mr. Ouyang $\times \times$ in the surname of a hundred families. This surname contains the two characters Ou (equivalent to "1+1") Yang (equivalent to " $1+1 \times 1$ "), But if you call him Mr. Ou $(" 1+1$ ") $\times \times$ or Mr. Yang $(" 1+1 \times 1$ ") $\times \times$, it is a kind of disrespect for him. Thinking that " $1+2$ " is proof of " $1+1$ " or " $1+1 \times 1$ ", it is not understanding or disrespect of " $1+2$ ". " $1+2$ " just selects some parameters shared by " $1+1$ " and " $1+1 \times 1$ ".
3 Through the gradual simplification of formula (3), Hardy's even Goldbach conjecture (formula (1a)) was obtained 100 years ago.
(3)
$\Pi \frac{\mathrm{p}-1}{\mathrm{p}-2}\left(1-\frac{r}{\pi\left(N-p_{r}-1\right)}\right)(1 \pm \delta)$

the number of answers is more. If the $\mathrm{N}=6 \mathrm{n}+2=\mathrm{p}_{+}+\mathrm{p}_{+}$, the number of answers is relatively small, If the $N=6 n=p$ $++p_{-}=6 n$, the number of answers is relatively small.

It can be seen that in the formula $\frac{\pi^{2}(N)}{N} \sim$ $\frac{N}{\ln ^{2} N}$. It is a kind of "nominal value" or "indicated value", but the method of correction is also very simple. $\frac{\pi^{2}(N)}{N}(1 \pm \delta) \sim \frac{N}{\ln ^{2} N}(1 \pm \delta)$.
(1a) $\quad \mathrm{r}_{2}(\mathrm{~N}) \sim 1.3203 \frac{N}{\ln ^{2} N} \Pi \frac{\mathrm{p}-1}{\mathrm{p}-2}(1 \pm \delta)$
Excluding $\delta$, this is the simplified Hardy-Litwood conjecture (A) in the world.
"Science only recognizes the first, not the second." said Lu Bai, vice president of China R\&D at GlaxoSmith.

Because "From the tolerance formula of Goldbach conjecture to Hardy-Littlewood conjecture (A)" may not be easy to understand. The following Table 1 is a comparison of the experimental accuracy of formulas (2),(3).

Table 1. In the formula (3), the existence of details of this $\pm \delta$

| N | $\begin{gathered} {[0-\mathrm{N}]} \\ \text { test } \end{gathered}$ | Formula (2) count | For.(2) <br> accurate | $\begin{gathered} {\left[\mathrm{p}_{\mathrm{r}}+1, \mathrm{~N}-\mathrm{p}_{\mathrm{r}}-1\right]} \\ \text { test } \end{gathered}$ | Formula (3) count | For. (3) accurate | $\begin{gathered} \text { Details } \pm \delta \\ (1 \pm \delta) \text { function } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 128 | 6 | 10.2 | 1.7 | 6 | 7.1377 | 1.1889 | (1- $\delta$ ) ——can |
| 256 | 16 | 15.3 | 0.9562 | 14 | 11.8173 | 0.8441 | (1+ $\delta$ ) - can |
| 512 | 22 | 24.5 | 1.1136 | 18 | 20.1775 | 1.1210 | (1- $\delta$ ) --can |
| 1024 | 44 | 38.4 | 0.8727 | 38 | 32.7933 | 0.8630 | (1+ $\delta$ ) --can |
| 2048 | 50 | 61.8 | 1.236 | 44 | 56.5372 | 1.2849 | (1- $\delta$ ) --can |
| 4096 | 106 | 102.8 | 0.9698 | 96 | 95.1456 | 1.0090 | (1+ $\delta$-——no |
| 8192 | 152 | 170.7 | 1.123 | 148 | 161.4751 | 1.0910 | (1- $\delta$ ) --can |
| 16384 | 302 | 291.3 | 0.9646 | 296 | 280.3683 | 0.9472 | (1+ $\delta$ )--can |
| 32768 | 488 | 497.4 | 1.1093 | 480 | 483.627 | 1.0076 | (1- $\delta$ )——can |
| 65536 | 870 | 862.7 | 0.9916 | 860 | 846.7056 | 0.9845 | (1+ $\delta$ )-—can |
| 131072 | 1498 | 1512.5 | 1.0097 | 1486 | 1491.7763 | 0.9702 | (1-8) - no |
| 262144 | 2628 | 2666.9 | 1.0148 | 2596 | 2639.4874 | 1.0168 | (1+ $\delta$ - - no |
| 524288 | 4734 | 4742.1 | 1.0017 | 4702 | 4708.6924 | 1.0014 | (1- $\delta$ ) --can |
| 1048576 | 8478 | 8471.8 | 0.9994 | 8436 | 8430.3789 | 0.9993 | (1+ $\delta$ ) --can |
| 2097152 | 14942 | 15246.4 | 1.0204 | 14906 | 15193.2259 | 1.0193 | (1- $\delta$ ) --can |
| 19999996 | 105832 | 106581.7 | 1.0071 | 105725 | 106446.351 | 1.0068 | (1+ $\delta$ - - no |
| 24999998 | 129571 | 129506.8 | 0.9995 | 129461 | 129372.246 | 0.9993 | (1-ס) - no |
| 100000094 | 437445 | 438281.5 | 1.0019 | 437291 | 438075.599 | 1.0018 | (1- $\delta$ ) ——can |
|  |  | 18 average | $=1.0556$ |  | 18 average | $=1.0198$ |  |

Table 1 shows that in most cases, using detail $\pm \delta$ correction can improve the accuracy. From a development perspective, when $\mathrm{N} \rightarrow \infty$, the detail can be ignored. Table 1 and Figure 1 do not show specific values of $\delta$.

From the average of 18 points, formula (3) is slightly more accurate than the formula. I wonder what everyone thinks?

Figure 2 shows the trend of the accuracy curves of formulas (1), (2) and (3). The arrow in the figure indicates an abnormality in the accuracy curve.


Figure 1 The formula (III) is accurate, but the formula (Ca) is not accurate.


## 4 Discussion.

Some of the above content hopes to help everyone understand "From the tolerance formula of even Goldbach conjecture to Hardy-Littlewood conjecture (A)".

## References

[1]Google. http://www.google.com. 2020.
[2]Journal of American Science.
http://www.jofamericanscience.org. 2021.
[3]Life Science
http://www.lifesciencesite.com. 2021.
[4]http://www.sciencepub.net/nature/0501/10-0247-
mahongbao-eternal-ns.pdf.
[5]Ma H. The Nature of Time and Space. Nature
and science 2003;1(1):1-11.
doi:10.7537/marsnsj010103.01.
http://www.sciencepub.net/nature/0101/01-ma.pdf.
[6]Marsland Press. http://www.sciencepub.net. 2021.
[7]Marsland Press. http://www.sciencepub.org. 2021.
[8]National Center for Biotechnology Information, U.S. National Library of Medicine. http://www.ncbi.nlm.nih.gov/pubmed. 2021.
[9]Nature and Science.
http://www.sciencepub.net/nature. 2021.
[10]Wikipedia. The free encyclopedia. http://en.wikipedia.org. 2021

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