On The Prime Equations: $P, jP+k-j(j=1,\cdots,k-1)$

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Abstract: Using Jiang function we prove that there exist infinitely many primes P such that each $jP+k-j$ is a prime.

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Theorem. Let k be a given prime.

$$P, jP+k-j(j=1,\cdots,k-1) \tag{1}$$

There exist infinitely many primes P such that each of $jP+k-j$ is a prime.

Proof. We have Jiang function[1]

$$J_2(\omega)=\prod_P[P-1-\chi(P)], \tag{2}$$

where

$$\omega=\prod_P P,$$

$\chi(P)$ is the number of solutions of congruence

$$\prod_{j=1}^{k-1}(jq+k-j)\equiv 0 \pmod P, \tag{3}$$

$$q=1,\cdots,P-1.$$

From (3) we have $\chi(2)=0$, if $P<k$ then $\chi(P)=P-2$, $\chi(k)=1$, if $k<P$ then $\chi(P)=k-1$.

From (3) and (2) we have

$$J_2(\omega)=(k-2)\prod_{k<P}(P-k)\neq 0. \tag{4}$$

We prove that there exist infinitely many primes P such that each of $jP+k-j$ is a prime

We have the asymptotic formula [1]

$$\pi_k(N,2)=\left|\{P\le N: jP+k-j=prime\}\right|\sim\frac{J_2(\omega)\omega^{k-1}}{\phi^k(\omega)}\frac{N}{\log^k N}, \tag{5}$$

where $\phi(\omega)=\prod_P(P-1)$.

Note:

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