

**The New Prime theorem (16) :**  $P_j = (j)^n P + (k-j)^n, j=1, \dots, k-1$

Chun-Xuan Jiang

P. O. Box 3924, Beijing 100854, P. R. China. [jiangchunxuan@vip.sohu.com](mailto:jiangchunxuan@vip.sohu.com)

**Abstract:** Using Jiang function we prove that there exist infinitely many primes  $P$  such that each of  $(j)^n P + (k-j)^n$  is a prime. [Chun-Xuan Jiang. **The New Prime theorem(16)**  $P_j = (j)^n P + (k-j)^n, j=1, \dots, k-1$ . *Rep Opinion* 2018;10(1):41-42]. ISSN 1553-9873 (print); ISSN 2375-7205 (online). <http://www.sciencepub.net/report>. 8. doi:[10.7537/marsroj100118.08](https://doi.org/10.7537/marsroj100118.08)

**Keywords:** prime; theorem; function; number; new

**Theorem.** Let  $k$  be a given prime.

$$P_j = (j)^n P + (k-j)^n (j=1, \dots, k-1, n=1, 2, \dots) \quad (1)$$

There exist infinitely many prime  $P$  such that each of  $(j)^n P + (k-j)^n$  is a prime.

**Proof.** We have Jiang function[1]

$$J_2(\omega) = \prod_P [P-1 - \chi(P)] \quad (2)$$

where  $\omega = \prod_P P$ ,  $\chi(P)$  is the number of solutions of congruence

$$\prod_{j=1}^{k-1} [(j)^n q + (k-j)^n] \equiv 0 \pmod{P}, q=1, \dots, P-1. \quad (3)$$

From (3) we have  $\chi(2) = 0$ , if  $P < k$  then  $\chi(P) \leq P-2$ ,  $\chi(k) = 1$ , if  $k < P$  then  $\chi(P) \leq k-1$ .  
From (3) we have

$$J_2(\omega) \neq 0 \quad (4)$$

We prove that there exist infinitely many primes  $P$  such that each of  $(j)^n P + (k-j)^n$  is a prime.

Jiang function is a subset of Euler function:  $J_2(\omega) \subset \phi(\omega)$ . We have asymptotic formula

$$\pi_k(N, 2) = \left| \left\{ P \leq N : (j)^n P + (k-j)^n = \text{prime} \right\} \right| \sim \frac{J_2(\omega) \omega^{k-1}}{\phi^k(\omega)} \frac{N}{\log^k N} \quad (5)$$

where  $\phi(\omega) = \prod_P (P-1)$

Example 1. Let  $k=3$ . From (1) we have

$$P_1 = P + 2^n, \quad P_2 = 2^n P + 1 \quad (6)$$

We have Jiang function

$$J_2(\omega) = \prod_{5 \leq P} (P-3) \neq 0 \quad (7)$$

We prove that there exist infinitely many primes  $P$  such that  $P_1$  and  $P_2$  are all prime.

**Note:** This paper had been published as:

[Chun-Xuan Jiang. **The New Prime theorem (16)**  $P_j = (j)^n P + (k-j)^n, j=1, \dots, k-1$ . *Academ Arena* 2015;7(1s): 23-23]. (ISSN 1553-992X). <http://www.sciencepub.net/academia>. 16

**Reference**

1. Chun-Xuan Jiang, Jiang's function  $J_{n+1}(\omega)$  in prime distribution. <http://www.wbabin.net/math/xuan2.pdf>.  
<http://wbabin.net/xuan.htm#chun-xuan>.
2. Vinoo Cameron. **Prime Number 19, The Vedic Zero And The Fall Of Western Mathematics By Theorem.** *Nat Sci* 2013;11(2):51-52. (ISSN: 1545-0740).  
[http://www.sciencepub.net/nature/ns1102/009\\_15631ns1102\\_51\\_52.pdf](http://www.sciencepub.net/nature/ns1102/009_15631ns1102_51_52.pdf).
3. Vinoo Cameron, Theo Den otter. **PRIME NUMBER COORDINATES AND CALCULUS.** *Rep Opinion* 2012;4(10):16-17. (ISSN: 1553-9873).  
[http://www.sciencepub.net/report/report0410/004\\_10859report0410\\_16\\_17.pdf](http://www.sciencepub.net/report/report0410/004_10859report0410_16_17.pdf).
4. Vinoo Cameron, Theo Den otter. **PRIME NUMBER COORDINATES AND CALCULUS.** *J Am Sci* 2012;8(10):9-10. (ISSN: 1545-1003).  
[http://www.jofamericanscience.org/journals/am-sci/am0810/002\\_10859bam0810\\_9\\_10.pdf](http://www.jofamericanscience.org/journals/am-sci/am0810/002_10859bam0810_9_10.pdf).
5. Chun-Xuan Jiang. **Automorphic Functions And Fermat's Last Theorem (1).** *Rep Opinion* 2012;4(8):1-6. (ISSN: 1553-9873).
6. Chun-Xuan Jiang. **A New Universe Model.** *Academ Arena* 2012;4(7):12-13 (ISSN 1553-992X).
7. Chun-Xuan Jiang. **The New Prime theorem(16)**  $P_j = (j)^n P + (k-j)^n, j = 1, \dots, k-1$ . *Academ Arena* 2015;7(1s): 23-23]. (ISSN 1553-992X). <http://www.sciencepub.net/academia>. 16

5/1/2015