Application Of Linear Programming In A Manufacturing Company In Feed Masters, Kulende, Kwara State.

[1] Balogun .O.S. [2] Role .M.R., [3]Akingbade .T.J. and [1]Akinrefon .A.A.

[1]Department of Statistics and Operations Research, Modibbo Adama University of Technology, P.M.B. 2076, Yola, Adamawa State, Nigeria.
[2]Department of Administration NSCDC, Kwara Command, No.5 Adelodun Street, G.R.A. , Ilorin, Kwara State, Nigeria.
[3]Department of Mathematical Sciences, Kogi State University, Anyigba, Kogi State, Nigeria.
stapsalms@yahoo.com, rolexy4real@yahoo.com, afuapetoluse@yahoo.com

Abstract: Many companies were and are still established to derive financial profit. In this regard the main aim of such establishments is to maximize (optimize) profit. This research is on using Linear programming Technique to derive the maximum profit from production of feeds produced by Feeds Maters Limited, Ilorin, Kwara State. Linear Programming of the operations of the company was formulated and optimum results derived using Software that employed Simplex method. The result shows that two particular feeds should be produced even when the company should satisfy demands of the other - not - so profitable items in the surrounding of the company.
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1. Introduction

Company managers are often faced with decisions relating to the use of limited resources. These resources may include men, materials and money. In other sector, there are insufficient resources available to do as many things as management would wish. The problem is based on how to decide on which resources would be allocated to obtain the best result, which may relate to profit or cost or both. Linear Programming is heavily used in Micro-Economics and Company Management such as Planning, Production, Transportation, Technology and other issues. Although the modern management issues are error changing, most companies would like to maximize profits or minimize cost with limited resources. Therefore, many issues can be characterized as Linear Programming Problems (Sivarethinamohan, 2008).

A linear programming model can be formulated and solutions derived to determine the best course of action within the constraint that exists. The model consists of the objective function and certain constraints. For example, the objective of Feed Masters Limited, Ilorin is to produce quality feeds needed by its customers, subject to the amount of resources (raw materials) available to produce the products needed by their respective customers who should also not violate Standard Organization of Nigeria (SON). The problem then is on how to utilize limited resources to the best advantage, to maximize profit and at the sometime selecting the products to be produced out of the number of products considered for production that will maximize profit.

The research is aimed at deciding how limited resources, raw materials of Feed Masters Limited, Ilorin , Kwara State would be allocated to obtain the maximum contribution to profit. It is also aimed at determining the products that contribute to such profit.

The scope of the research is to use Linear Programming on some of the feeds produced by Feed Masters Limited, Ilorin. The data on which this is based are quantity of raw materials available in stock, cost and selling prices and therefore the profit of each product. The profit constitutes the objective function while raw materials available in stock are used as constraints. If demands which must be met are to be available, such can be included in the constraints. The data is secondary data collected in the year 2007 at the Feed Masters Limited, Ilorin, Kwara State.

The Simplex method, also called Simple technique or Simplex Algorithm, was invented by George Dantzig, an American Mathematician, in 1947. It is the basic workhorse for solving Linear Programming Problems up till today. There have been many refinements to the method, especially to take advantage of computer implementations, but the essentials elements are still the same as they were when the method was introduced (Chinneck, 2000; Gupta and Hira, 2006).

The Simplex method is a Pivot Algorithm that transverses the through Feasible Basic Solutions while Objective Function is improving. The Simplex method is, in practice, one of the most efficient algorithms but it is theoretically a finite algorithm only for non-degenerate problems (Feiring, 1986).

To derive solutions from the LP formulated using the Simplex method, the objective function and the constraints must be standardized.
The characteristics of the standard form are:

(i) All the constraints are expressed in the form of equations except the non-negativity constraints which remain inequalities (≥ 0).

(ii) The right-hand-side of each constraint equation is non-negative.

(iii) All the decision variables are non-negative.

(iv) The Objective function is of maximization or minimization type. Before attempting to obtain the solution of the linear programming problem, it must be expressed in the standard form is then expressed in the "the table form" or "matrix form" as given below:

$$Maximize \;\; Z = \sum_{j=1}^{r} C_j X_j$$

$$Subject \quad to$$

$$\sum_{j=1}^{r} a_{ij} X_j \leq b_i, \; (b_i \geq 0), \; i = 1,2,3,\ldots,m$$

$$X_j \geq 0, \; j = 1,2,3,\ldots,m$$

In standard form (Canonical form), it is

$$Maximize \;\; Z = \sum_{j=1}^{r} C_j X_j$$

$$Subject \quad to$$

$$\sum_{j=1}^{r} a_{ij} X_j + S_i = b_i, \; i = 1,2,3,\ldots.,m$$

$$X_j \geq 0, \; j = 1,2,3,\ldots.,n$$

$$S_i \geq 0, \; i = 1,2,3,\ldots.,m$$

Any vector X satisfying the constraints of the Linear Programming Problems is called Feasible Solution of the problem (Fogiel, 1996; Schulze, 1998; Chinneck, 2000).

1.1 Algorithm to solve linear programming problem:

(i) See that all $b_i's$ are positive, if a constraint has negative b_i multiply it by -1 to make b_i positive.

(ii) Convert all the inequalities by the addition of slack or by subtraction of surplus variable as the case may be.

(iii) Find the starting Basic Feasible Solution.

(iv) Construct the Simplex table as follows:

Basic Variable	E_j	X_1	X_2	$X_3\ldots.$	X_n	y_1	$y_2\ldots$	y_m	X_b
y_1	0	a_{11}	a_{12}	$a_{13}\ldots$	a_{1m}	1	0	0	b_1
y_2	0	a_{21}	a_{22}	$a_{23}\ldots$	a_{2m}	0	1	0	b_2
y_3	0	a_{31}	a_{32}	$a_{33}\ldots$	a_{3m}	0	0	1	b_m
	Z_j	Z_1	Z_2	Z_3	Z_4	0	0	0	$Z = Z_0$
	E_j	E_1	E_2	E_3	E_4	0	0	0	
	.	.	.	.	.	.	.	.	
$\Delta b_j = Z_j - E_j$		ΔX_1	ΔX_2	$\Delta X_3\ldots$	ΔX_n	Δy_1	$\Delta y_2\ldots$	Δy_m	

(v) Testing for optimality of Basic Feasible Solution by computing $\Delta Z_j - E_j$. If $Z_j - E_j \geq 0$, the solution is optimal; otherwise, we proceed to the next step.

(vi) To improve on the Basic Feasible Solution, we find the basic matrix. The variable that corresponds to the most negative of $Z_j - E_j$ is the INCOMING VECTOR while the variable that corresponds to the minimum ratio b_i / a_{ij} for a particular j, and $a_{ij} \geq 0$, $i = 1, 2, 3, \ldots, m$ is the OUTGOING VECTOR.

(vii) The key element or the pivot element is determined by considering the intersection between the arrows that corresponds to both incoming and outgoing vectors. The key element is used to generate the next table. In the next table, pivot element is replaced by UNITY, while all other elements of the pivot column are replaced by zero. To calculate the new values for all other elements in the remaining rows of that first column, we use the relation.

New row = Former element in old rows − (intersection element in the old row) × (Corresponding element of replacing row).

$(viii)$ Test of this new Basic Feasible Solution for optimality as (6) it is not optimal; repeat the process till optimal solution is obtained. This was implemented by the software Management Scientist Version 6.0.

Table 1: Quantity of raw materials available in stock for month

Raw Materials	Quantity Available per month (kg)
Maize	20000
G.N.C	15000
Soya Beans	25000
Lime Stone	10000
Bone	14000
Wheat Offal	15500
Maize Offal	15500
Fish Offal	8000
Lysine	1000
Methionine	1000
Salt	8000
Layer Premix	2000
Broiler Premix	75
Chick Premix	75

Table 2: Quantity of raw materials needed to produce a unit each product

	PRODUCT				
Raw Material	Chick Mash (kg)	Layer Mash (kg)	Grower Mash (kg)	Broiler Starter Mash (kg)	Broiler Finisher Mash (kg)
Maize	11	11	8	11	10
G.N.C	3	3	2	5	3.5
Soya Beans	4.5	3	8	5	4.5
Lime Stone	0	2	0.5	0	0
Bone	1	0.5	0.5	1.5	0.5
Wheat Offal	5	6.5	4	1.6	5
Maize Offal	0	0	2.5	0	0
Fish Offal	0.5	0.5	0	1	1
Lysine	0.05	0.05	0.05	0.03	0.03
Methionie	0.05	0.05	0.05	0.03	0.03
Salt	0.07	0.075	0.075	0.07	0.07
Layer Premix	0	0.075	0	0	0
Broiler Premix	0	0	0	0.07	0.07
Chick Premix	0.07	0	0.075	0	0

Table 3: Average Cost and Selling of a crate of each product

Product	Average Cost price(₦)	Average Selling price(₦)	Profit(₦)
Chick Mash	966.55	1300	333.45
Layer Mash	898.88	1200	301.12
Grower Mash	697.63	1000	302.37
Broiler Starter Mash	1142.35	1350	207.65
Broiler Finisher Mash	1013.75	1325	311.25

1.2 Model Formulation

$$Maximize\ Z = 333.45X_1 + 301.12X_2 + 302.37X_3 + 207.65X_4 + 311.25X_5$$

$$Subject\ to$$

$$11X_1 + 11X_2 + 8X_3 + 11X_4 + 10X_5 \leq 20000$$
$$3X_1 + 3X_2 + 2X_3 + 5X_4 + 3.5X_5 \leq 15000$$
$$4.5X_1 + 3X_2 + 8X_3 + 5X_4 + 4.5X_5 \leq 25000$$
$$2X_1 + 0.5X_5 \leq 10000$$
$$X_1 + 0.5X_2 + 0.5X_3 + 1.5X_4 + 0.5X_5 \leq 14000$$
$$5X_1 + 6.5X_2 + 4X_3 + 1.6X_4 + 5X_5 \leq 15500$$
$$2.5X_3 \leq 15000$$
$$0.5X_1 + 0.5X_2 + X_4 + X_5 \leq 8000$$
$$0.05X_1 + 0.05X_2 + 0.05X_3 + 0.03X_4 + 0.03X_5 \leq 1000$$
$$0.05X_1 + 0.05X_2 + 0.05X_3 + 0.03X_4 + 0.03X_5 \leq 1000$$
$$0.07X_1 + 0.075X_2 + 0.075X_3 + 0.07X_4 + 0.07X_5 \leq 8000$$
$$0.075X_2 \leq 2000$$
$$0.07X_4 + 0.07X_5 \leq 75$$
$$0.07X_4 + 0.075X_5 \leq 75$$
$$For\ \ X_i \geq 0, i = 1, 2, 3, \ldots, 5$$

Now, introducing the slack variable to convert inequalities to equations, it gives:

$$Maximize\,Z = 333.45X_1 + 301.12X_2 + 302.37X_3 + 207.65X_4 + 311.25X_5$$

$$Subject\ to$$

$$11X_1 + 11X_2 + 8X_3 + 11X_4 + 10X_5 + X_6 = 20000$$
$$3X_1 + 3X_2 + 2X_3 + 5X_4 + 3.5X_5 + X_7 = 15000$$
$$4.5X_1 + 3X_2 + 8X_3 + 5X_4 + 4.5X_5 + X_8 = 25000$$
$$2X_1 + 0.5X_5 + X_9 = 10000$$
$$X_1 + 0.5X_2 + 0.5X_3 + 1.5X_4 + 0.5X_5 + X_{10} = 14000$$
$$5X_1 + 6.5X_2 + 4X_3 + 1.6X_4 + 5X_5 + X_{11} = 15500$$
$$2.5X_3 + X_{12} = 15000$$
$$0.5X_1 + 0.5X_2 + X_4 + X_5 + X_{13} = 8000$$
$$0.05X_1 + 0.05X_2 + 0.05X_3 + 0.03X_4 + 0.03X_5 + X_{14} = 1000$$
$$0.05X_1 + 0.05X_2 + 0.05X_3 + 0.03X_4 + 0.03X_5 + X_{15} = 1000$$
$$0.07X_1 + 0.075X_2 + 0.075X_3 + 0.07X_4 + 0.07X_5 + X_{16} = 8000$$
$$0.075X_2 + X_{17} = 2000$$
$$0.07X_4 + 0.07X_5 + X_{18} = 75$$
$$0.07X_4 + 0.075X_5 + X_{19} = 75$$
$$For\ X_i \geq 0, i = 1, 2, \ldots, 19$$

Where,
X_1 = 25kg of Chick mash
X_2 = 25kg of Layers mash
X_3 = 25kg of Growers mash
X_4 = 25kg of Broiler starter mash
X_5 = 25kg of Broiler finisher mash

2. Analysis and Result
Optimal Solution
Objective function value = 668,367.36

Variables	Value
X_1	0.000
X_2	181.818
X_3	1000.000
X_4	0.000
X_5	1000.000

The Management Scientist Version 6.0 gives:
$Z = 668,367\ X_2 = 182,\ X_3 = 1000\ and\ X_5 = 1000$

3. Interpretation of Result

Based on the data collected the optimum results derived from the model indicate that three products should be produced 25kg of Layers mash, 25kg of Grower mash and 25kg of Broiler finisher mash. Their production quantities should be 182, 1000 and 1000 units respectively. This will produce a maximum profit of ₦668,367.

4. Conclusion

Based on the analysis carried out in this research and the result shown, Feed Master Limited, Ilorin should produce 25kg of Chick mash, 25kg of Layer mash, 25kg of Grower mash, 25kg of Broiler starter mash and 25kg of Broiler finisher mash but more of 25kg of Layer mash, 25kg of Grower mash and 25kg of Broiler finisher mash in order to satisfy their customers. Also, more of 25kg of Layer mash, 25kg of Grower mash and 25kg of Broiler finisher mash should be produced in order to attain maximum profit because they contribute mostly to the profit earned.

Correspondence to:
Balogun Oluwafemi Samson
c/o Department of Statistics and Operations Research, Modibbo Adama University of Technology, P.M.B. 2076, Yola, Adamawa State. Nigeria
Telephone: +2348035217339
Emails: stapsalms@yahoo.com

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